

**NUMS Physics Handmade Notes by Farah**

Fluid Dynamics (Chap # 6) bit

study of fluids in motion

\* Fluid → any substance that can flow is called as fluid.

Viscosity

Frictional effect b/w the layers of a flowing fluid.

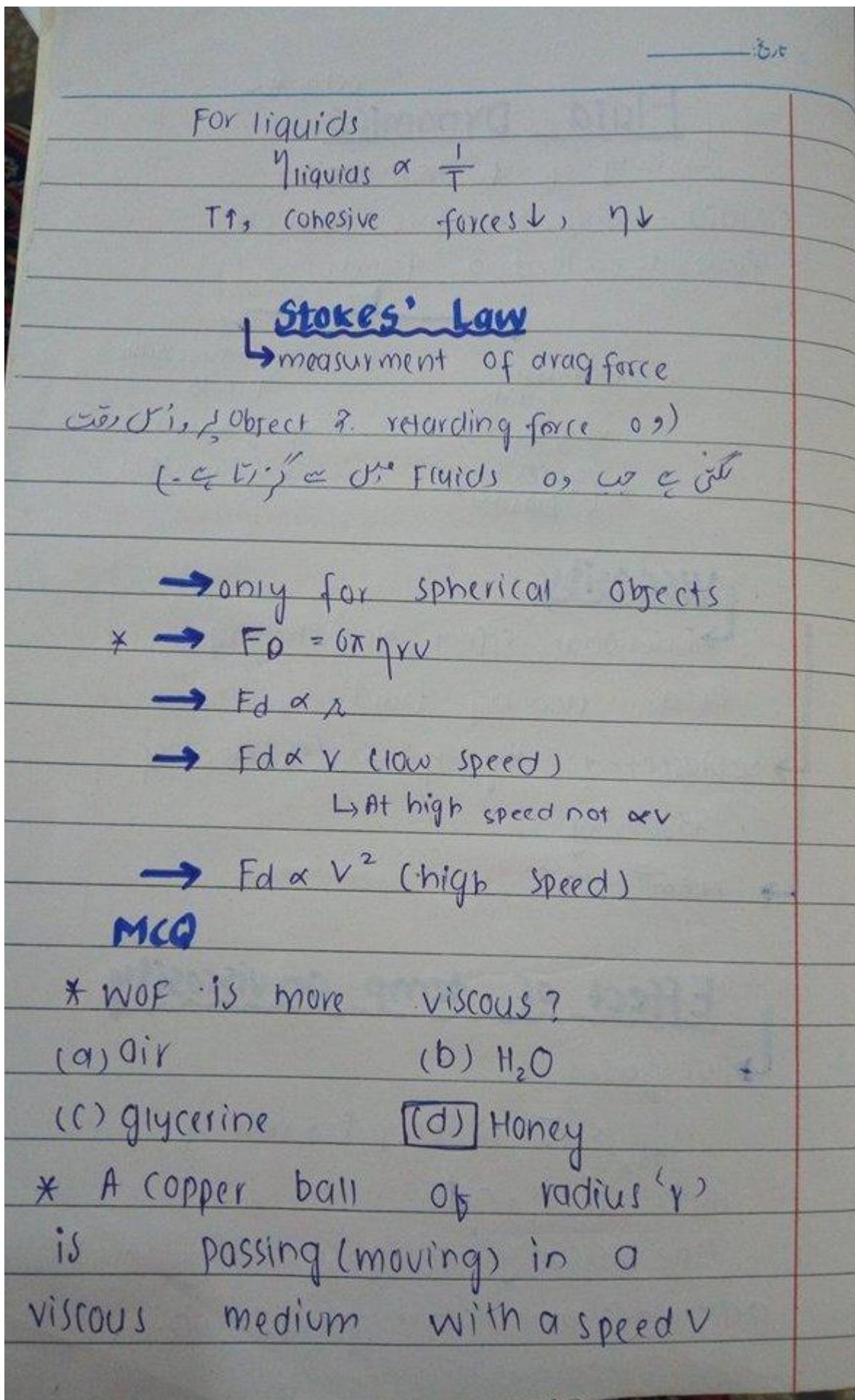
→ represented by ' $\eta$ ' → co-efficient of viscosity  
 $\text{N s m}^{-2}$ ,  $\text{Pas}$

Effect of temp on viscosity

For gases

$\eta_{\text{gases}} \propto T \Rightarrow \text{Temp} \uparrow, \text{rate of diffusion} \uparrow, \eta \uparrow$

The viscosity of gases is dependant on rate of diffusion.



having drag force  $F$ . Another 'Cu' Ball of radius  $r' = 2r$  and  $v' = 2v$  will have drag force?

$$F_D = 6\pi\eta(2r \times 2v)$$

(a)  $F$       (b)  $2F$       (c)  $F/2$       (d)  $4F$

$F' = 4F$

**(Imp)**

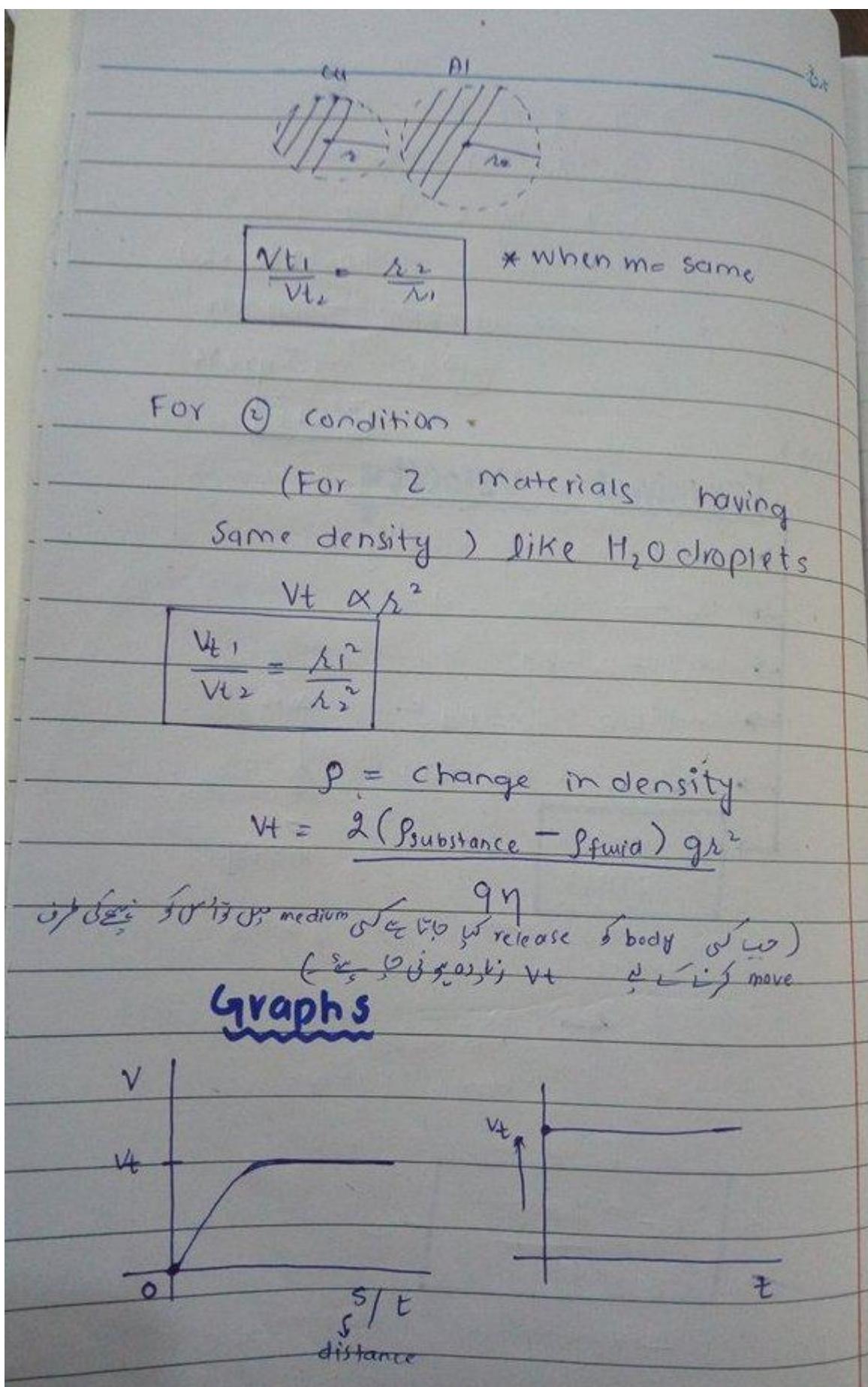
**Terminal velocity**

- max constant velocity
- $v_t \rightarrow \text{Gain}, a=0$
- $F_{\text{net}} = W - F_d$
- $F_{\text{net}} = 0 \quad W = F_d$
- $F_d = W \rightarrow \text{terminal vel.}$
- $$v_t = \frac{mg}{6\pi\eta rv} \quad \textcircled{1}$$
- For diff. materials having same masses.

due to inertia ← again move downward ← Body )  
When  $F_d = W$

\* 
$$v_t = \frac{2\rho gr^2}{9\eta} \quad \textcircled{2}$$

For  $\textcircled{1} \rightarrow \text{condition}$



\* Two water droplets are falling through air have ratio of radii 2:3. What will be ratio of their Vts?

$$\frac{V_{t1}}{V_{t2}} = \frac{r_1^2}{r_2^2}$$

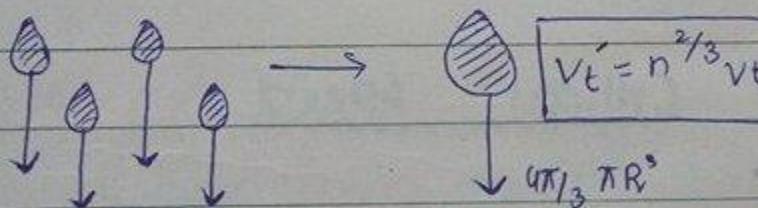
(a) 9:4

(b) 4:9

(c) 2:3

(d) 3:2

### Effect of Combined Terminal velocities



$$V_t' = n^{2/3} V_t$$

$$V_t' = (4)^{2/3} (5)$$

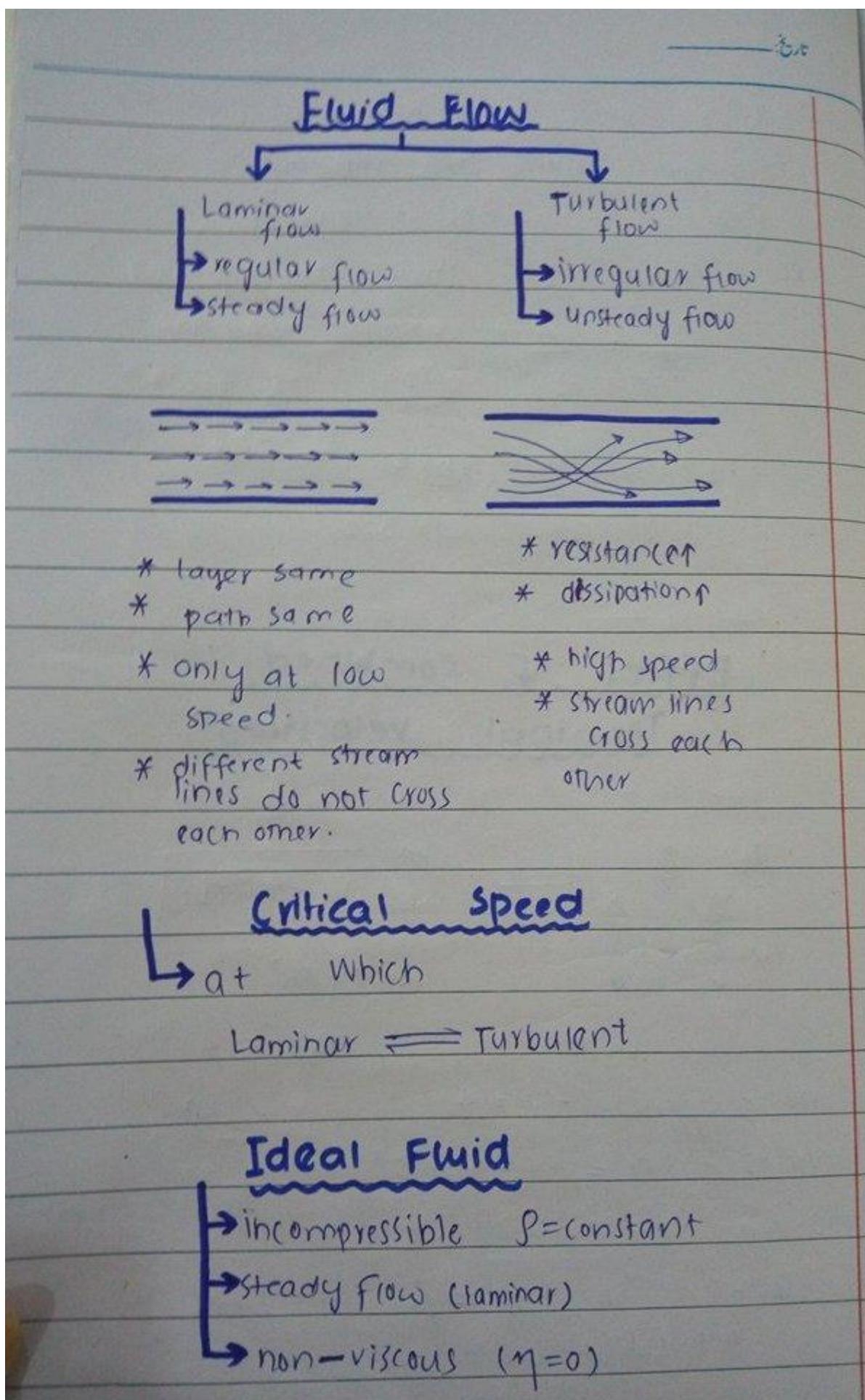
no of droplets =  $n = 4$ 

$$V_t = (2)^{2/3} (5)$$

$$V_t \text{ of each droplet} = V_t = 5 \text{ cm s}^{-1}$$

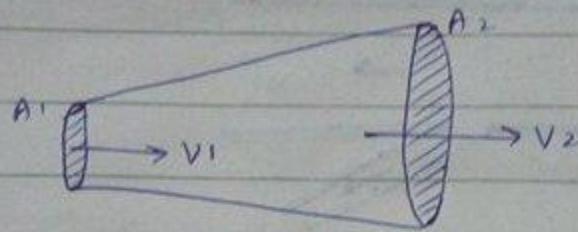
$$V_t = (16)^{2/3} (5) \text{ cm s}^{-1}$$

Terminal speed of big droplet = ?



## Equation of continuity

→ explains law of conservation  
of mass



\* VOLUME FLOW RATE =  $\frac{V}{t} = AV$

\* UNITS =  $AV = m^3 s^{-1}$

\*  $A_1V_1 = A_2V_2$

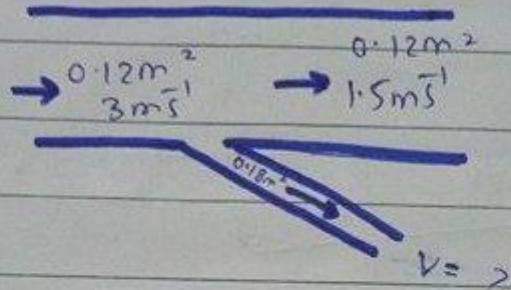
$$\star \frac{V_1}{V_2} = \frac{A_2}{A_1} \rightarrow \frac{V_1}{V_2} = \frac{r_2^2}{r_1^2} \rightarrow \frac{V_1}{V_2} = \frac{d_2^2}{d_1^2}$$

\* Water is flowing through a tube of non-uniform cross-sectional area.

if the radii of tube at entrance and exit are in the ratio 3:2 then ratio of velocity of liquid entering and leaving the tube is?

(a) 1 : 1      (b) 4 : 9  
 (c) 9 : 4      (d) 1 : 27

\*



(a)  $1 \text{ ms}^{-1}$       (b)  $2.25 \text{ ms}^{-1}$   
 (c) 1.25      (d)  $2 \text{ ms}^{-1}$

$$A_1 V_1 = A_2 V_2 + A_3 V$$

$$V = \frac{A_1 V_1 - A_2 V_2}{A_3}$$

$$V = \frac{0.12 \text{ m}^2 \times 3 \text{ ms}^{-1} - 0.12 \text{ m}^2 \times 1.5 \text{ ms}^{-1}}{0.18 \text{ m}^2}$$

## Bernoulli's Equation

→ explain law of conservation

of energy

$$* P_1 + \frac{1}{2} \rho V_1^2 + \rho g h_1 = P_2 + \frac{1}{2} \rho V_2^2 + \rho g h_2$$

$$\star P + \frac{1}{2} \rho V^2 + \rho g h = \text{constant}$$

$$\star P + \frac{\frac{1}{2} \rho V^2}{V} + \frac{\rho g h}{V} = \text{constant}$$

$\star$  Xply with V

$$\star PV + \frac{1}{2} \rho V^2 + \rho gh = \text{constant}$$

### MCQ

\* WOF is Pressure?

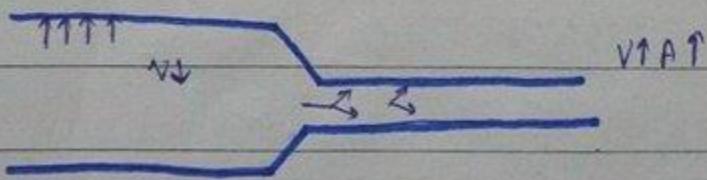
(a) P → static

(b)  $\frac{1}{2} \rho V^2$  → dynamic pressure

(c)  $\rho gh$  → pressure with depth

(d) all.

Same physical quantities are added.



$$\uparrow P + \frac{1}{2} \rho V^2 = \text{constant}$$

enough time to exert pressure.

pressure → Dynamic

enough time to exert pressure.

Past paper question

\* water is flowing through a horizontal pipe of non-uniform cross-sectional area  $\Delta p \cdot E = 0$

WOF is correct?

(a)  $P + \rho v^2 = \text{constant}$

(b)  $2P + 2\rho v^2 = \text{constant}$

(c)  $2P + \rho v^2 = \text{constant}$

(d)  $2P + 2\rho = \text{constant}$

$P + \frac{1}{2} \rho v^2 = \text{constant}$

$2P + \rho v^2 = \text{constant}$

## Applications of Bernoulli's Equation

### Torricelli's Theorem

\* depth from surface reference point

\* height earth reference point

$v = \sqrt{2g(h_1 - h_2)}$

$h_1 - h_2 = h = \text{depth}$

$$V = \sqrt{2gh}$$

$$V \propto \sqrt{h}$$

\*  $V = ?$

$$V = \sqrt{2gh} =$$

$$V = \sqrt{2 \times 10 \times 5}$$

$$= \sqrt{100} = 10 \text{ m/s}$$

(a) 10 m/s (b) 20 m/s (c) 30 m/s  
(d) 40 m/s

\*  $\rightarrow V_D > V_C > V_B > V_A$

$$V \propto \sqrt{h}$$

$V \uparrow \propto \text{depth} \uparrow$

$\rightarrow h_D > h_C > h_B > h_A$

## Range of Efflux

$$S = vt$$

$$R = \sqrt{2gH_1} \times \sqrt{\frac{2H_2}{g}}$$

$$R = \sqrt{\frac{4g(H_1 H_2)}{g}}$$

$$R = 2\sqrt{H_1 H_2}$$

$$Y = \frac{1}{2}gt^2$$

\* Vacuum no medium so the  $F_D$  will be zero and  $V_t = 0$ .  
 \* speed of sound in vacuum is zero.

$$V_t = \frac{mg}{6\pi \eta r} \rightarrow \text{size same}$$

$V_t \propto mg$



more mass  
weight ↑

← Fe Al

\* Viscous force on a spherical body moving through a fluid do not depend on mass.

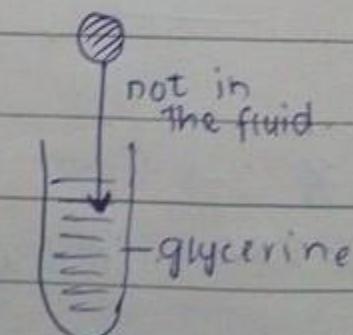
$$F_D = 6\pi \eta r v$$

$$* F_{net} = w - F_d \\ = 10 - 0$$

$$10 = \\ F_{net} = w - F_d$$

$$= 10 - 2 \\ 8 = F_{net}$$

$$6 = 10 - 4$$



$\downarrow F_{net} \downarrow$   
 $w = \text{remains}$   
 $\text{same}$

$F_D \propto \frac{1}{F_{net}}$

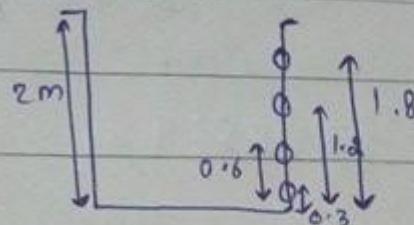
$$4 = 10 - 6$$

$$2 = 10 - 8$$

$$0 = 10 - 10$$

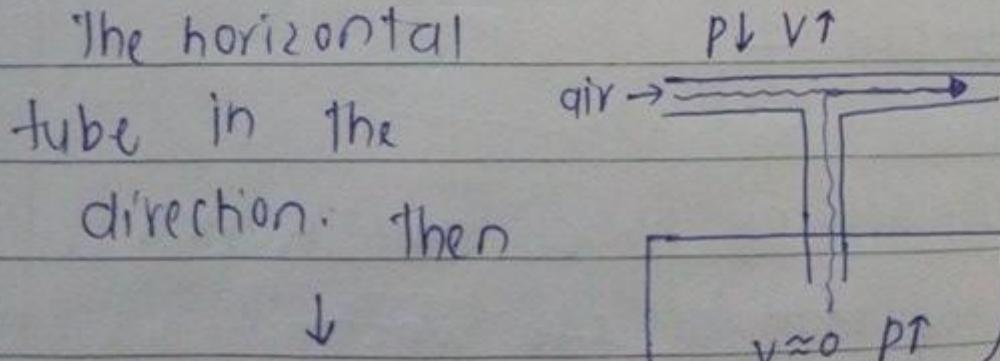
decrease =  $F_d$  $F_{net} \downarrow$ 

\*  $V \propto \frac{1}{\text{height}}$



\* diastolic pressure, flow of blood is laminar 75-80 torr.

\* Water stands at level B in the capillary tube in the arrangement shown in figure. If a jet of air is blown into the horizontal tube in the direction. Then



\* rise above level B in capillary tube.

$$V \approx 0 \text{ PT}$$

$$\begin{aligned} * V_t &= \frac{mg}{6\pi\eta R} \quad V_t \propto \frac{m}{R} \\ \frac{V_{t1}}{V_{t2}} &= \frac{m_1}{m_2} \times \frac{R_2}{R_1} \\ &= \frac{5}{3} \times \frac{5}{3} = \frac{25}{9} = 25:9 \end{aligned}$$

$$V_{t1} : V_{t2} = 25:9$$

\* Pressure of fluid is low where stream lines are closer to each other.



$$\frac{V_1}{V_2} = \frac{r_2^2}{r_1^2}$$

$$V_2 \propto \frac{1}{r_2} \quad V_2 \propto \left(\frac{1}{r}\right)^2$$

$$4V_2 \propto \frac{1}{\left(\frac{r}{2}\right)^2}$$

\* carburetor of motor car works on Bernoulli's equation.

\* let the 90000 kg mass of pure water falls on the pulley of the turbine in 1.5 min to

run the generator. flow rate?

$$AV = \text{flow rate}$$

$$AV = V/t = \frac{90}{90} = 1 \text{ m}^3 \text{ s}^{-1}$$

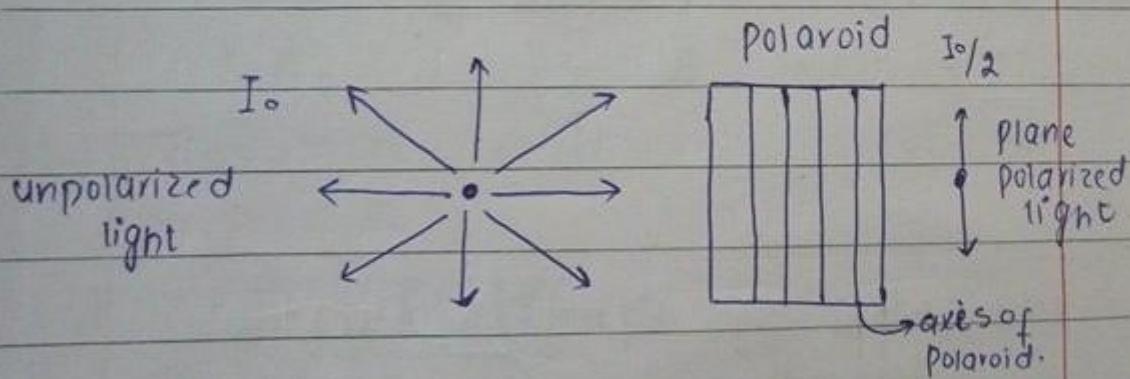
$$\rho = m/v$$

$$= \frac{90,000}{1000} = 90$$

$$V = m/\rho$$

## Unit #4 polarization

→ Confining of light beam in a single plane is called polarization.



## Malus Law

$$I = I_0 \cos^2 \theta$$

↳ applicable only for plane polarized light

MCG

\* A polaroid is placed in front of a plane polarized light. Now if we give a polaroid a rotation of  $45^\circ$  what will be the  $I$  of emergent ray if max  $I_0$  of ray.

(a) $I_0$	(b) $I_0/2$
(c) $\frac{I_0}{\sqrt{2}}$	(d) $\frac{I_0}{4}$

\* polarization of light proves that

(a) particle nature of light      (b) Quantum nature of light

(c) transverse wave nature of light      (d) longitudinal wave nature of light

\* Sound waves can never be

polarized.

\* Plane polarized light is passed through a polaroid. On viewing through the polaroid we find that when the polaroid is given one complete rotation.

- (a) The intensity gradually becomes zero and remains zero
- (b) There is no change in intensity of light
- (c) Remains maximum
- (d) intensity of light varies such that it becomes twice max and twice zero.

## LIGHT

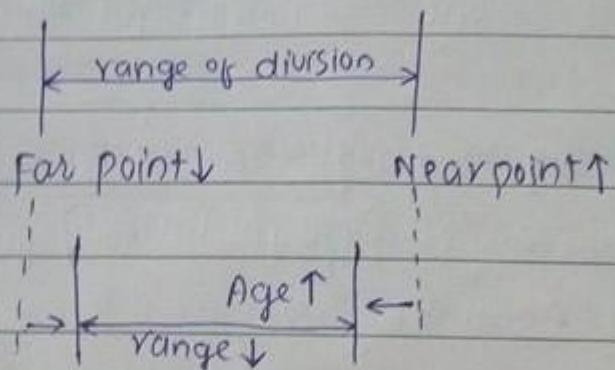
Near Point | Least distance of distinct vision ( $d = 25\text{cm}$ )

- normal healthy person  $d = 25\text{cm}$
- newborn baby 5-7 cm
- with increase in age this
- (d) also increase.

Far point

↳ infinity  $\infty$  for healthy  
normal person.  
→ age increase it decreases.

Range of vision

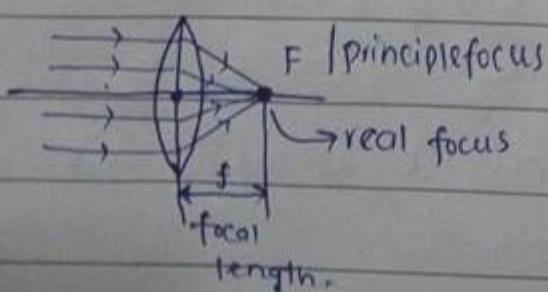
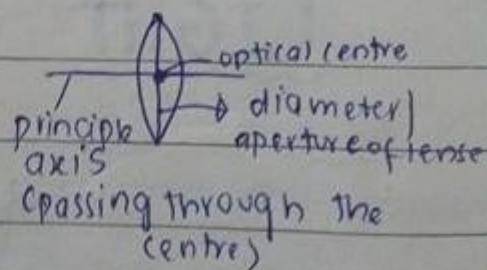


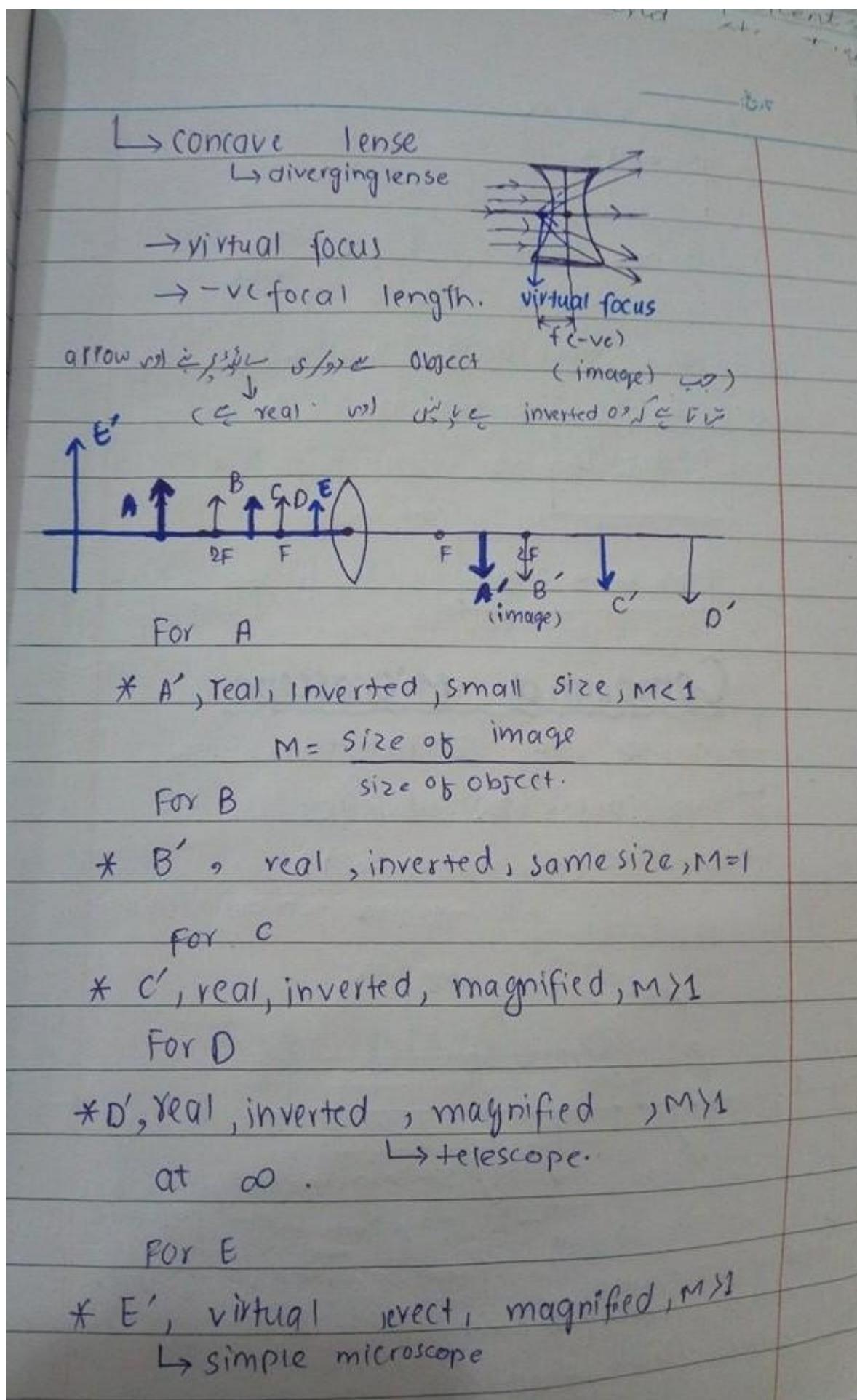
## Ray Diagrams

### Lenses

↳ convex lens

↳ converging





8.5

simple microscope

$$\hookrightarrow M = \frac{d}{f}$$

$d = \text{near point}$        $f = \text{focal length of lens}$

At  $\infty$  (when image is at  $\infty$ )

$$M_{\infty} = \frac{d}{f}$$

$$M = 1 + M_{\infty}$$

Compound Microscope

- consist of 2 lenses (convex)
- eye piece (towards eye)
- objective (towards object)

$f_e \uparrow$   $f_o \downarrow$

final image / 2nd image  
Nature w.r.t original object  
(inverted, virtual, magnified)

(within the focal length of)  
1st image | intermediate eye piece  
(real, inverted, magnified)

nature with respect to 1st / intermediate image.

(virtual, erect, magnified)

### Length of Microscope

The distance b/w two lenses.

$$* M = \frac{q}{p} (1 + d/f_e)$$

$$* M = \frac{L}{f_o} (1 + d/f_e)$$

$$* M = M_1 M_2$$

### Lens Formula

$$\frac{1}{f_o} = \frac{1}{p} + \frac{1}{q}$$

The diagram shows a lens in the center. An arrow pointing towards the lens from the left is labeled "object" above the lens and "p" below the lens. An arrow pointing away from the lens to the right is labeled "image" below the lens and "q" below it.

### Test Discussion

$$R = \frac{D}{1.22 \lambda} \rightarrow \begin{matrix} \text{Diameter} \\ \text{wavelength of light.} \end{matrix}$$

resolving power

magnification have no units.

$$f_e = 5 \text{ cm.}$$

$$M = M_o \times M_e$$

$$M = M_o (1 + d/f_e)$$

$$M_{\text{Compound}} = 30$$

$$M_o = \frac{M_{\text{compound microscope}}}{1 + d/f_e}$$

$$= \frac{30}{(1 + 25/5)} = \frac{30}{5} = 6$$

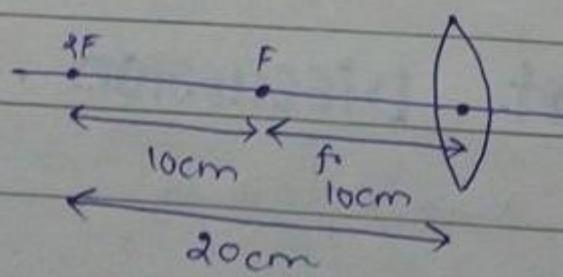
\* The normal human eye can focus a sharp image of an obj on the eye, is located at any where b/w  $\infty$  and near point (25cm)

\* Magnifying power of compound microscope

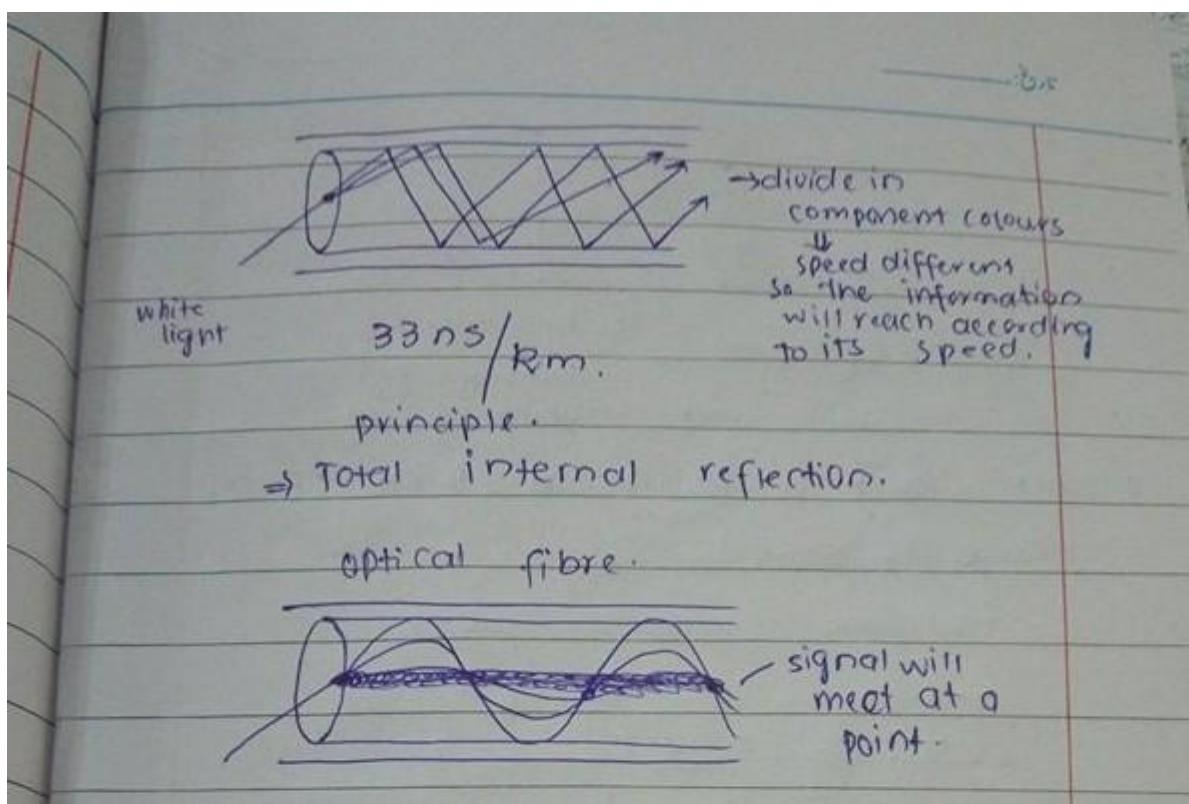
= Objective magni.  $\times$  eye piece mag.

$$M = M_o \times M_e$$

\* An object is placed at 20cm from a lens whose focal length is 10cm. the final image will form at 20cm.



\* Multimode Step index fiber.



\* A <sup>size</sup> 2mm object is placed at 20cm from a converging lens of 10cm focal length.  
The size of image is at 2m.

## VIBGYOR

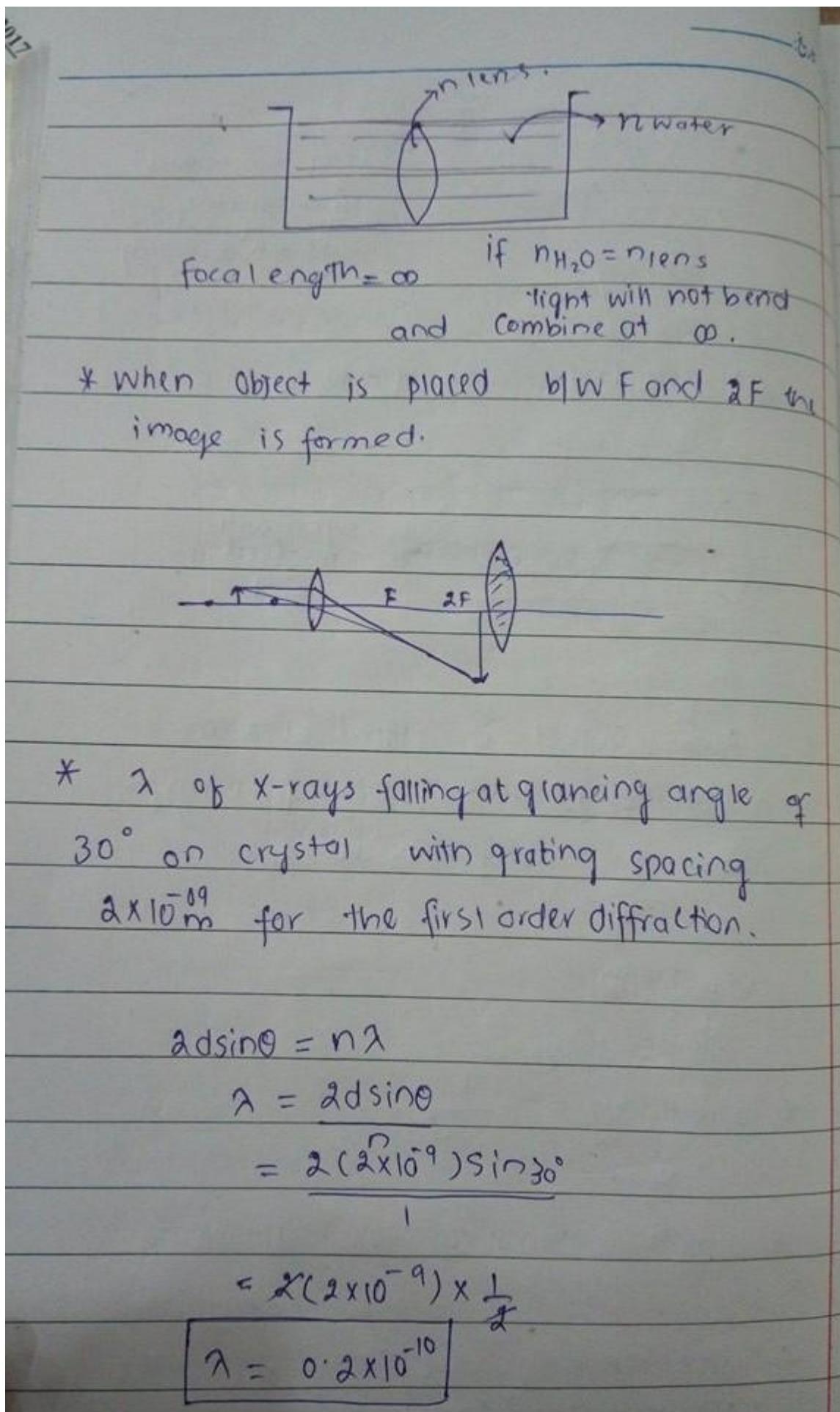
visible to eye ↴

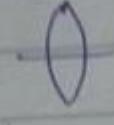
$$\text{* Scattering} \propto \frac{1}{\lambda^4}$$

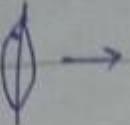
$$R \propto \frac{1}{\lambda}$$

\* most sensitive colour is yellow to eye.

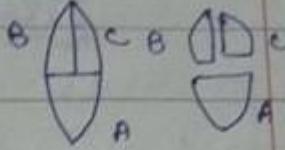
\* light bend due the difference in refractive index.




 no difference of focal length or thickness.

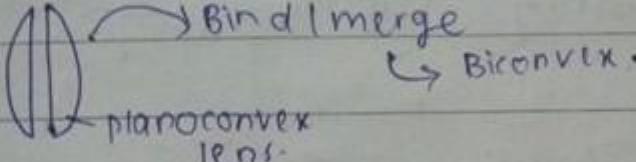

 → differ. in thickness.

$f \propto \frac{1}{\text{thickness}}$

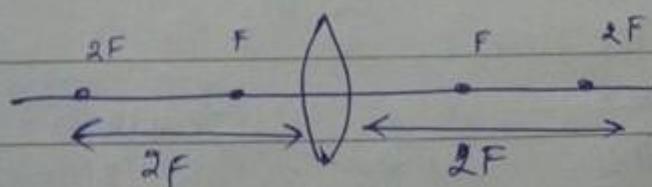


power  $\propto \frac{1}{\text{focal length}}$

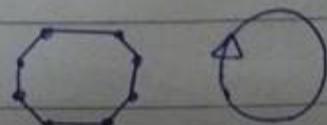
\* Biconvex lens / double convex lens:


 Biconvex  
 lens.

\* distance b/w obj and image is never less than  $4F$  minimum.



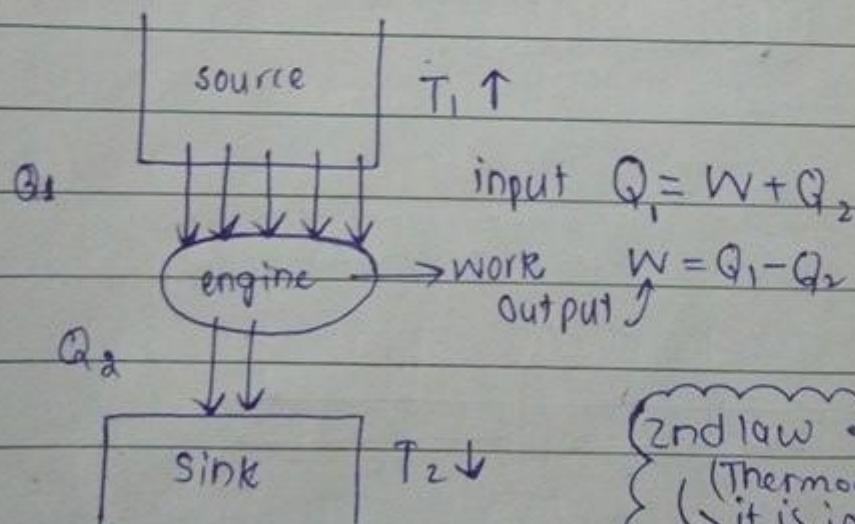
\*  $P = \frac{100}{f(\text{cm})}$ ,  $P = \frac{1}{f(\text{m})}$   
 Power.

\* 
 $\theta = 2\pi/8 \text{ rad.} = 2(180)/8 = \pi/4$   
 $360^\circ 2\pi \text{ rad.}$   
 rotation.

\*  $n = c/v$  less than  $c$   
in medium.

## Heat Engine

- device
- heat energy → mechanical energy
- working ?
- Source of heat  $T_1 \uparrow \uparrow$
- Sink (rejected heat)  $T_2 \downarrow \downarrow$
- working substance (engine)



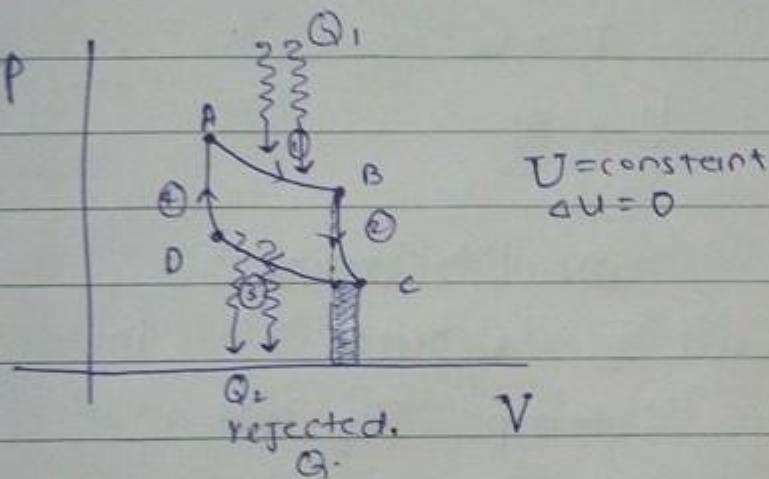
$W$  = output

$Q_1$  = input

{ 2nd law of  
(Thermodynamics)  
it is impossible  
to devise an  
engine that converts  
all heat into work. }

## Carnot Engine /cycle

- ① → isothermal expansion
- ② → adiabatic expansion
- ③ → isothermal compression
- ④ → adiabatic compression.



isothermal expansion  $\rightarrow Q_1$  heat

absorbed.

isothermal compression  $\rightarrow Q_2$  rejected.

\* efficiency  $\eta = \eta = 1 - \frac{T_2}{T_1}$

\*  $\eta = \frac{\text{output}}{\text{input}}$

$$= \frac{W}{Q_1}$$

\*  $\eta = \frac{Q_1 - Q_2}{Q_1} = 1 - \frac{Q_2}{Q_1}$

$$* \eta = \left(1 - \frac{T_2}{T_1}\right) 100$$

$$* \eta = 1 - \frac{T_2}{T_1}$$

$$\frac{W}{Q_1} = 1 - \frac{T_2}{T_1}$$

$$\Rightarrow T \propto Q$$

$$\Rightarrow \frac{T_1}{T_2} = \frac{Q_1}{Q_2}$$

Carnot engine

\* Efficiency depends on the two temp. of sink and source.

\* The efficiency of Carnot engine can be 100% at 0 Kelvin.

\* 0 Kelvin is not possible.

### MCQs

\* A Carnot engine is operating b/w  $27^\circ C$  and  $-123^\circ C$ . What will be  $\eta$  of this engine.

	T(K) t(°C)
(a) 0.75	3.5
(b) 0.4	273 123
(c) 0.5	150 300
(d) 1	150 300

$\eta = 1 - \frac{T_2}{T_1}$

$$T_2 = -123 + 273 \text{ K} \\ = 150 \text{ K}$$

$$\eta = 1 - \frac{150}{300} = \frac{300 - 150}{300} = \frac{150}{300} = 0.5$$

$$T_1 = 300 \text{ K}$$

\* A carnot engine is operating b/w two temp 300K and 600K. if the output work is 800J . Then the absorbed heat by engine is?

$$\frac{W}{Q_1} = 1 - \frac{T_2}{T_1} \quad \frac{Q_1}{Q_2} = \frac{T_1}{T_2}$$

$$\frac{800}{Q_1} = 1 - \frac{600}{300} = \frac{300 - 600}{300} = \frac{-300}{300} = -1$$

$$\frac{800}{Q_1} = \frac{600}{300} = \frac{300 - 600}{300} = \frac{-300}{300} = -1$$

(a) 1200J      (b) 1600J       $Q_2 = 800 \times 2 = 1600 \text{ J}$   
 (c) 200J      (d) 2400J

\* A Carnot engine takes 300 cal of heat at 500K and rejects 150 cal of heat to sink. The temperature of sink will be.

(a) 1000K      (b) 750K  
(c) 500K      (d) 250K

$$\frac{T_1}{T_2} = \frac{Q_1}{Q_2}$$

$$T_1 \oplus T_2 = T_1 \otimes T_2$$

Q1

$$= \frac{500k(300)_{cal}}{150\text{ cal}}$$

$$= 250k$$

\* A Carnot engine is operating

b/w two temp  $42^{\circ}\text{C}$  and  $27^{\circ}\text{C}$

What will be the  $\eta$  of this engine?

$$1.7 = \left(1 - \frac{T_2}{T_1}\right) 100.$$

$$\begin{aligned}
 &= \left( 1 - \frac{300K}{700K} \right) \times 100. \\
 &= \left( \frac{700 - 300}{700} \right) \times 100 \\
 &= \frac{400}{700} \times 100 \\
 &\therefore \eta = 57\%
 \end{aligned}$$

35

○ ○  
 62.7  
 $\frac{273}{700K}$   
 $\frac{273}{27}$   
 $\frac{27}{27 - 1K}$

[4]

### Test Discussion (5+6)

The frequency of light having wavelength  $3 \times 10^{-5} \text{ cm}$ .

$$f = c/\lambda = \frac{3 \times 10^8}{3 \times 10^{-5}} = 10^{8+5} = 1 \times 10^{13} \text{ Hz}$$

\* %age error =  $\frac{332 - 280}{332} \times 100 \approx 16\%$

\* In all real process where heat, the energy available for doing useful work decreases entropy increases.

\*  $V = \sqrt{\frac{\gamma P_1}{P_2}}$        $P = \frac{1}{3} \rho V^3$   
 $\gamma P \propto \rho V$

\* entropy  $\uparrow \Leftrightarrow$  more available heat  $\rightarrow$  increase  
 hot cold  
 Sand + Salt entropy  $\uparrow$   
 available heat  $\downarrow$

Short cut

\*  $T_f(K) = n^2 T_i(K)$   
 $n = \text{no of times}$

$T_f(K) = (2)^2 \times (283K)$   
 $= 4 \times 283$   
 $T_f(K) = 1132K$

\* At what temp the velocity of sound in air is two times its velocity at  $10^\circ C$

Laplace  $\epsilon = \frac{Ea}{\gamma p^2}$

\*  $v = \sqrt{\frac{\gamma p}{\rho}} = \sqrt{\frac{Ea}{\rho}}$

$v \propto \sqrt{Ea}$

$\frac{Ea}{E_i} = \frac{\gamma p}{P} = \gamma = C_p/C_v$   
 ↴ newtons

$E_i = \text{Isothermal modulus of elasticity} = P_{ext}$

\* density of dry air =  $1.29 \text{ kg m}^{-3}$

density of moist air =

By volume the gases are more  $\text{N}_2 \text{ O}_2$ .

dry air  $28 + 32 = 60 \text{ amu}$ .

moist air  $28 + 32 = 60 \text{ amu}$  of mass  $V \rho$   
replace  $\text{H}_2\text{O}$   $\rightarrow$   $-6 \text{ K}_c$

$\beta = m/V$  dry air  $m \uparrow \rho \uparrow$

moist air Volume = same

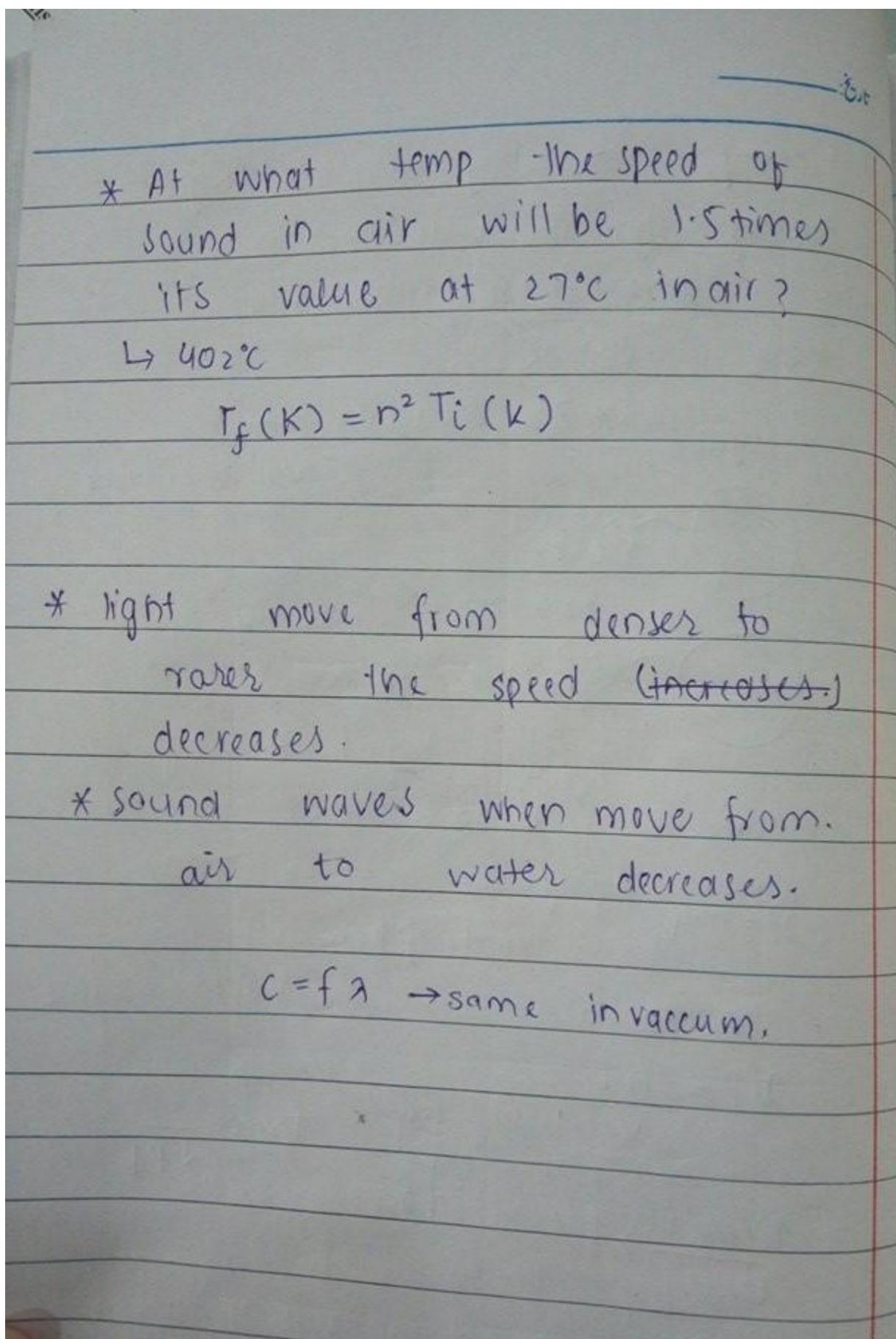
$$\uparrow \rho = \frac{m}{V}$$

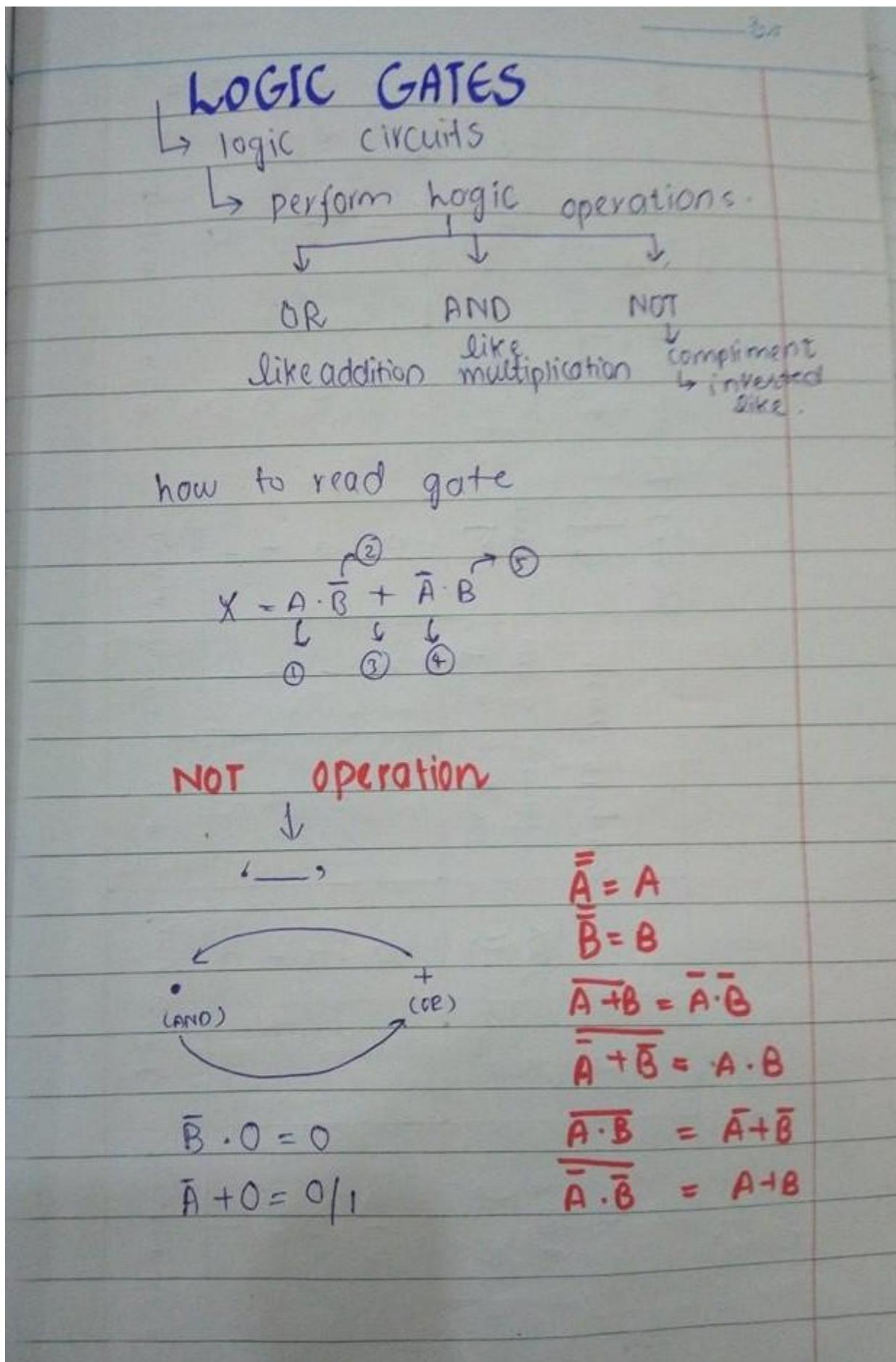
$$\frac{\uparrow V_{\text{moist}}}{\downarrow V_{\text{dry}}} > 1$$

$$V = \sqrt{\frac{\rho P}{\rho_0}}$$

$$TV \propto \frac{1}{\sqrt{P}}$$

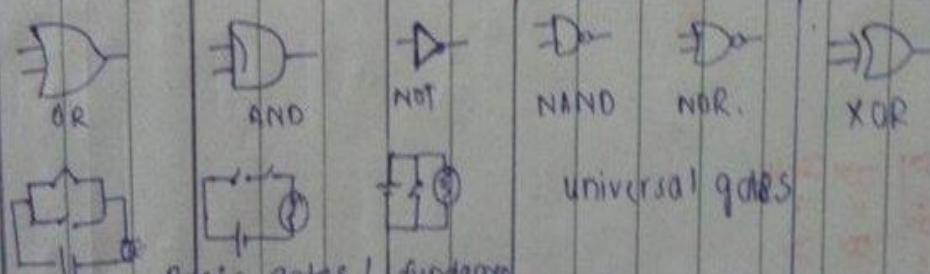
\* velocity of sound in vacuum is zero and sound wave is a mechanical wave.





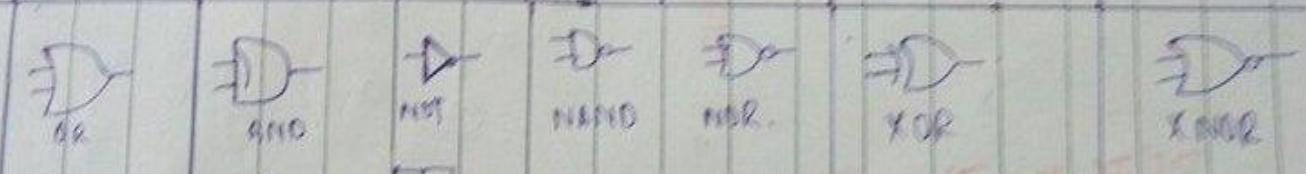
A	B	$X_1 = A + B$	$X_2 = A \cdot B$	$X_3 = \bar{A}/B$ ONLY B	$X_4 = \bar{A} \cdot \bar{B}$	$X_5 = \bar{A} \cdot \bar{B}$	$X_6 = A \cdot \bar{B} + \bar{A} \cdot B$	$X_7 = A \cdot B + \bar{A} \cdot \bar{B}$
0	0	0	0	1	1	1	0	1
0	1	1	0	1	1	0	1	0
1	0	1	0	0	1	0	1	0
1	1	1	1	0	0	0	0	1

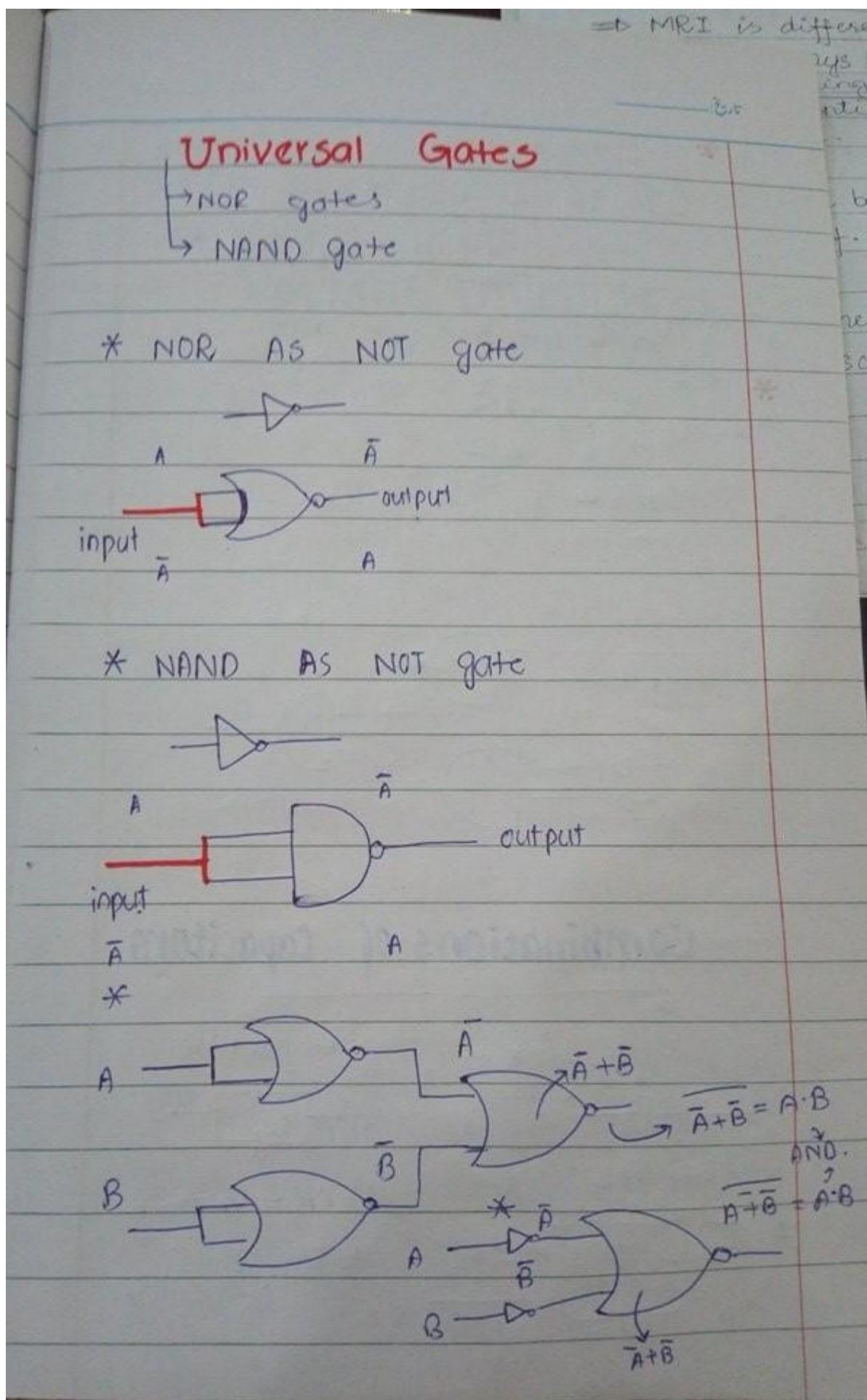
Basic gates / fundamental

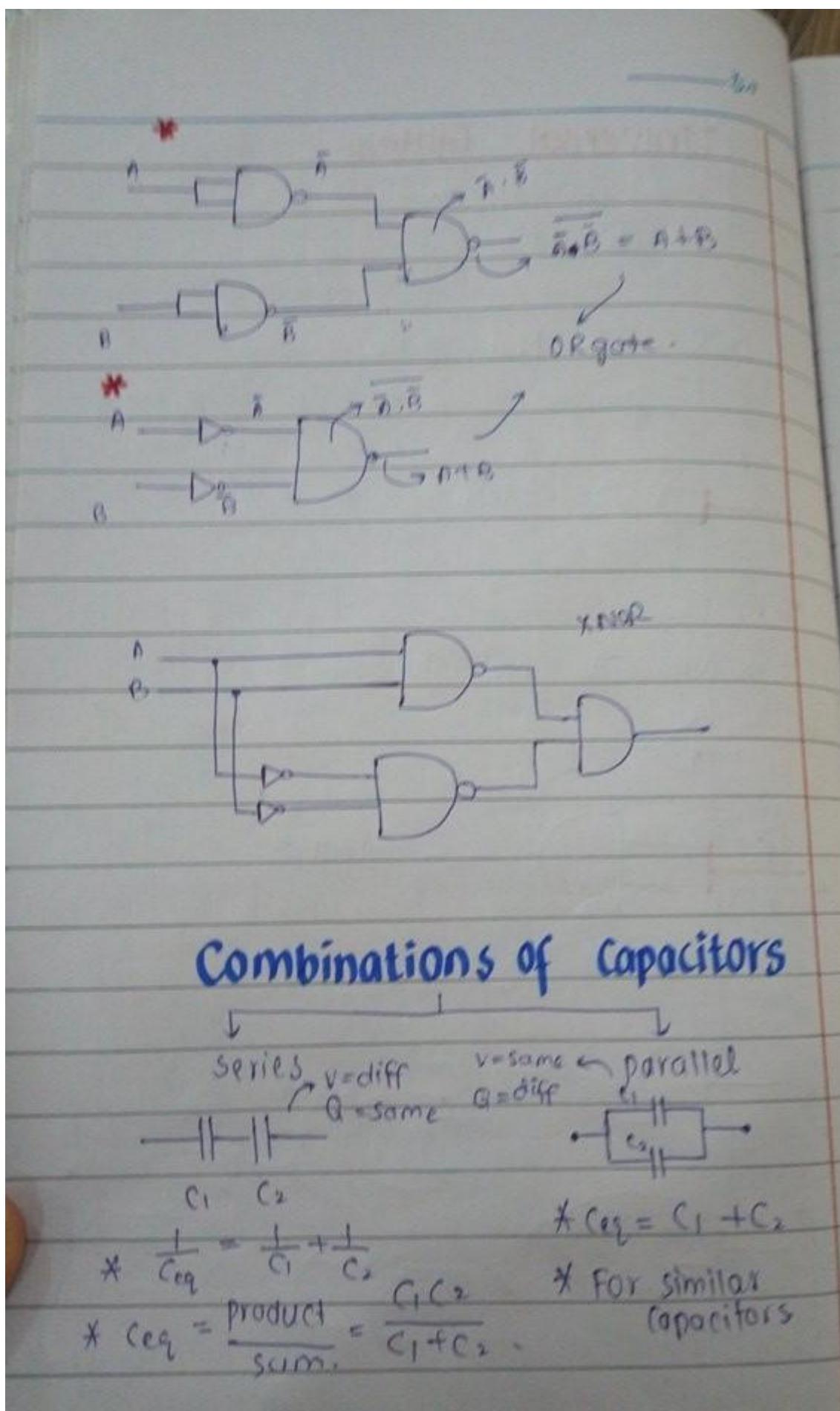


A	B	$X_1 = A + B$	$X_2 = A \cdot B$	$X_3 = \bar{A}/B$ ONLY B	$X_4 = \bar{A} \cdot \bar{B}$	$X_5 = \bar{A} \cdot \bar{B}$	$X_6 = A \cdot \bar{B} + \bar{A} \cdot B$	$X_7 = A \cdot B + \bar{A} \cdot \bar{B}$
0	0	0	0	1	1	1	0	1
0	1	1	0	1	1	0	1	0
1	0	1	0	0	1	0	1	0
1	1	1	1	0	0	0	0	1

Basic gates / fundamental





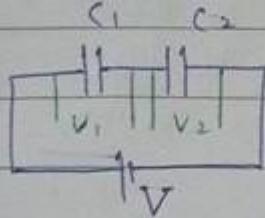


For similar capacitor  $\star C_{eq} = nC$

$$C_{eq} = \frac{C}{n} \rightarrow n \text{ no. of capacitors.}$$

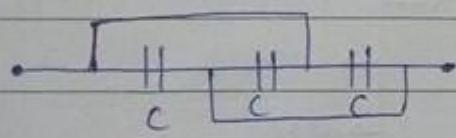
### VOLTAGE DIVISION IN CAPACITOR

(Only for series due to diff. V)



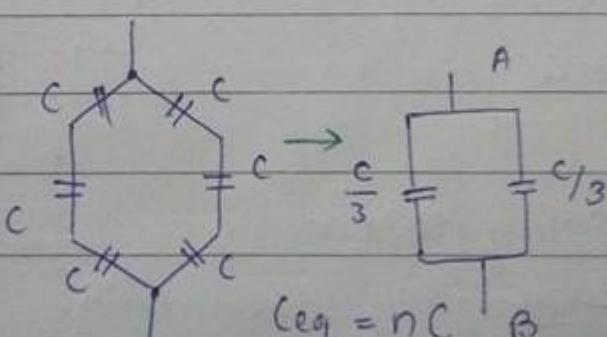
$$V_1 = \frac{C_2}{C_1 + C_2} \times V$$

$$V_2 = \frac{C_1}{C_1 + C_2} \times V$$

\* 

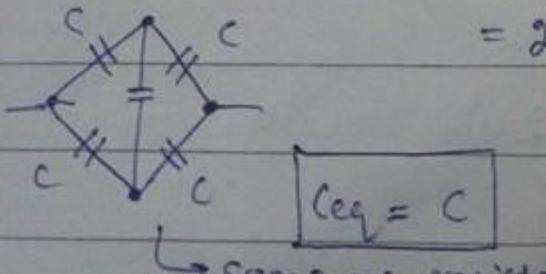
parallel

$$C_{eq} = nC = 3C$$

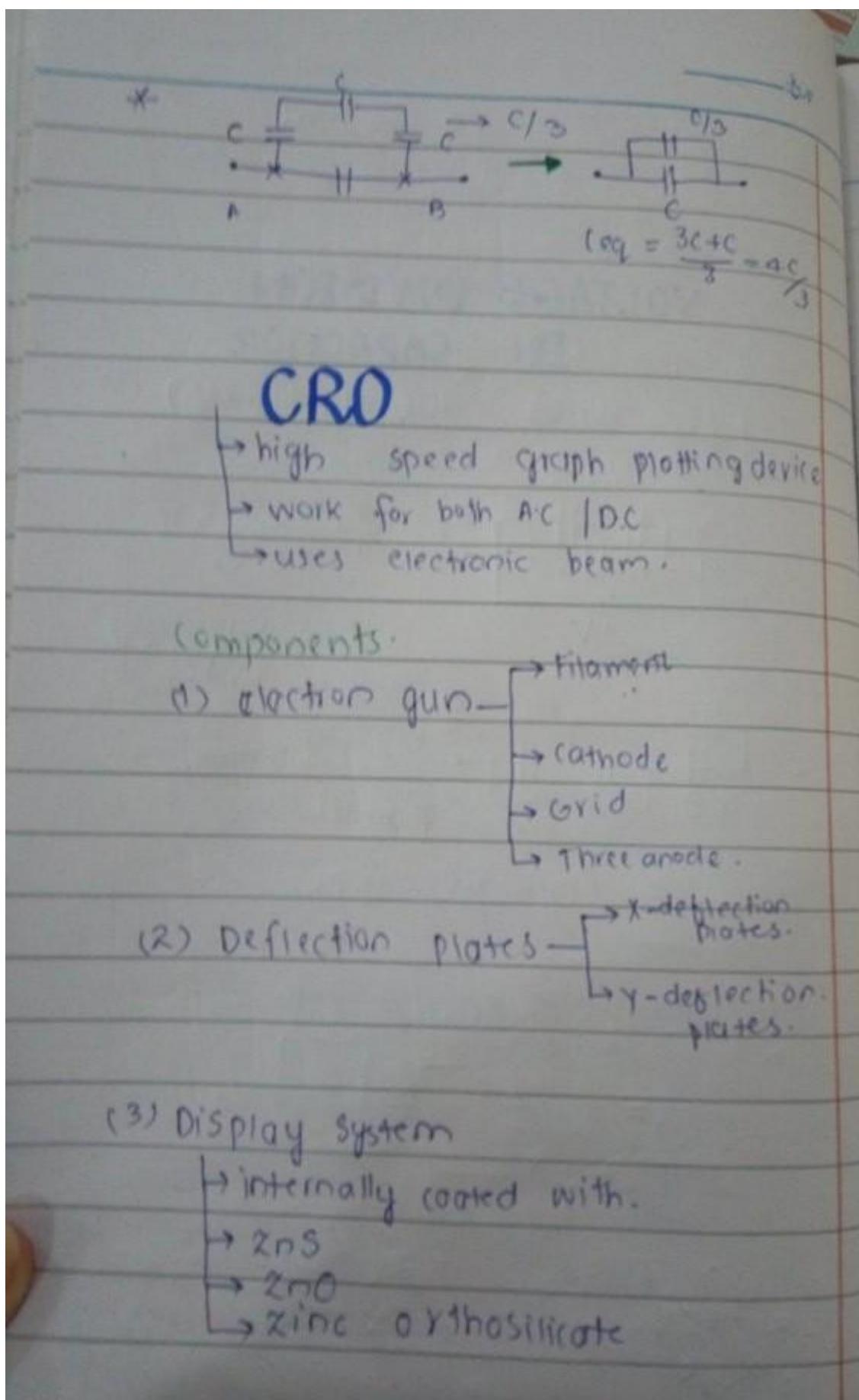
\* 

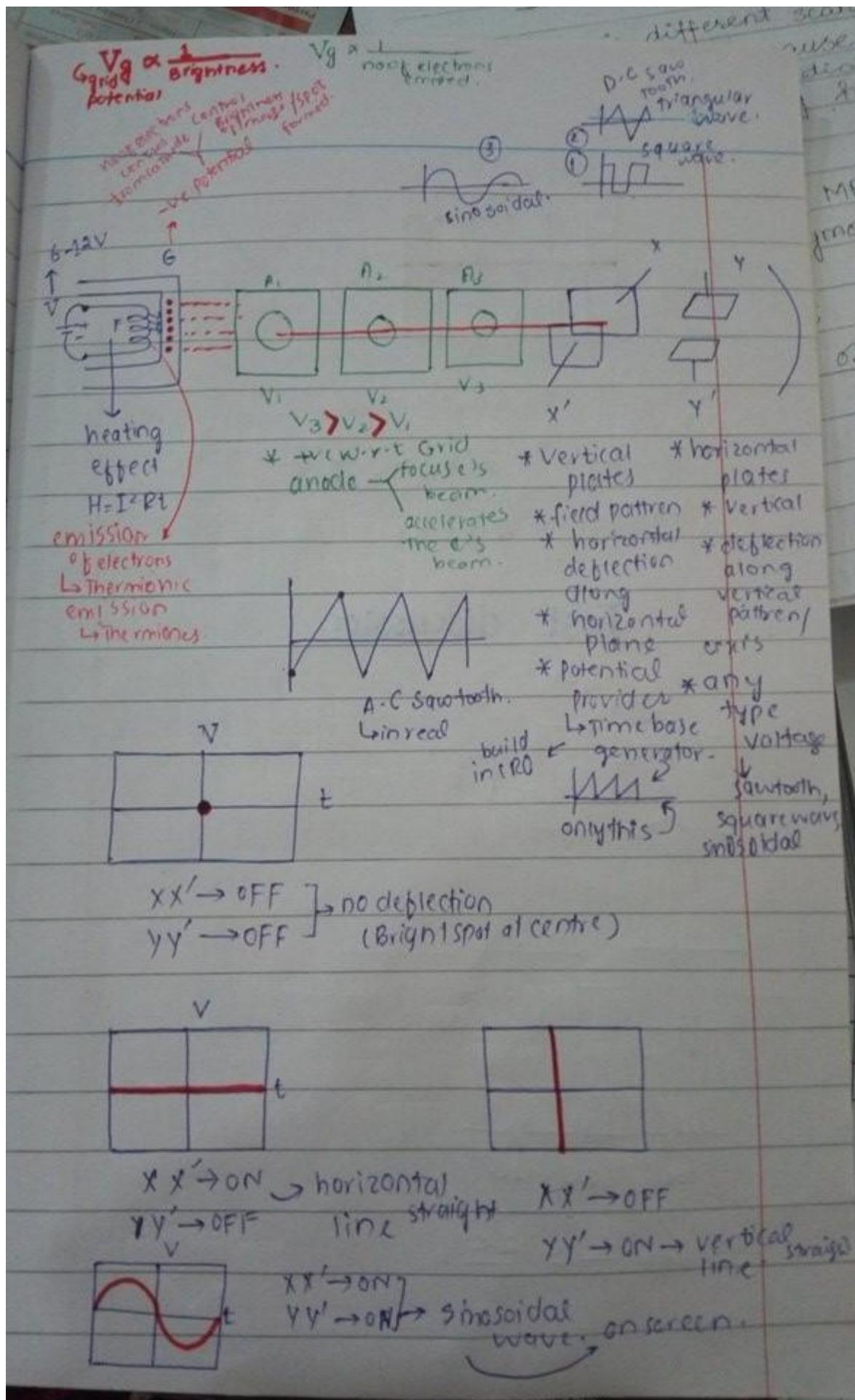
$$(C_{eq} = nC) \rightarrow \frac{C}{3} = \frac{C}{3}$$

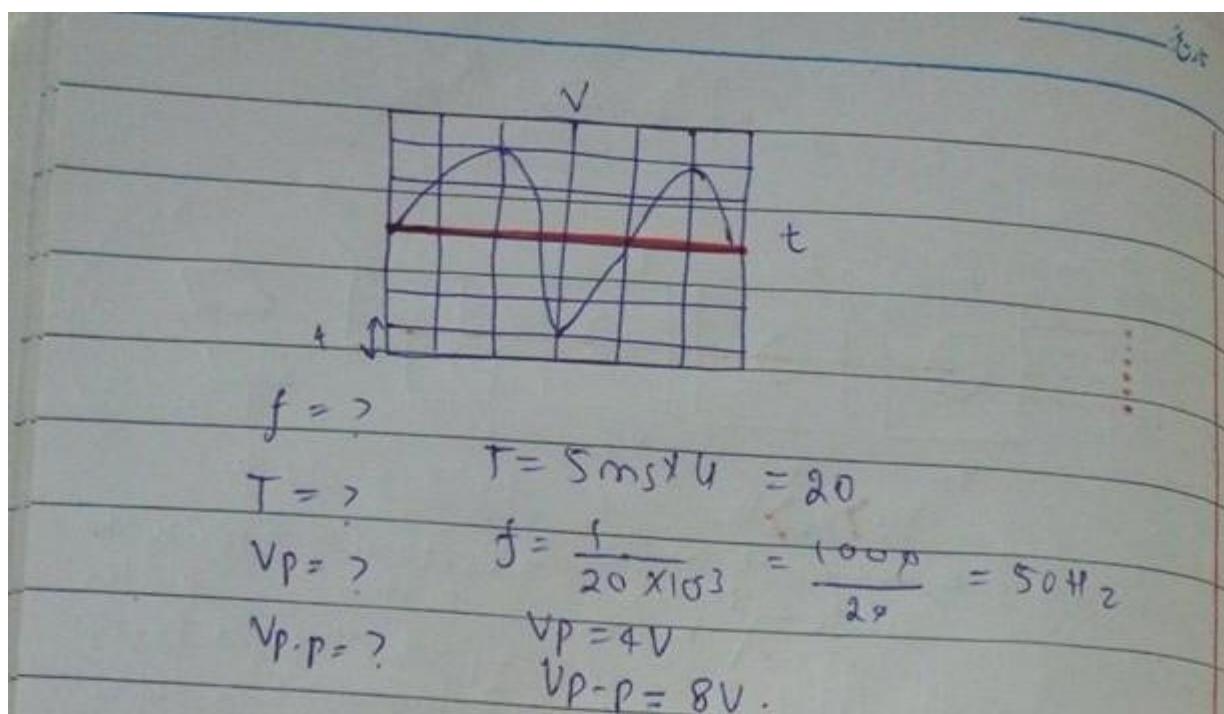
$$= 2(\frac{C}{3}) = \frac{2C}{3}$$



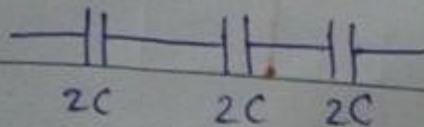
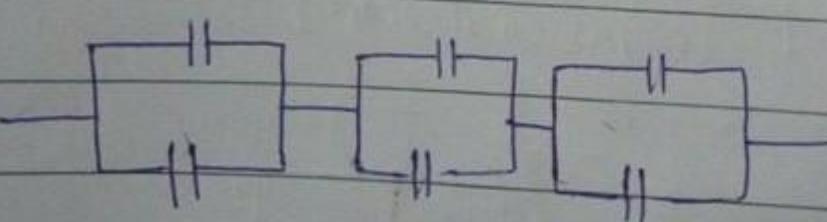
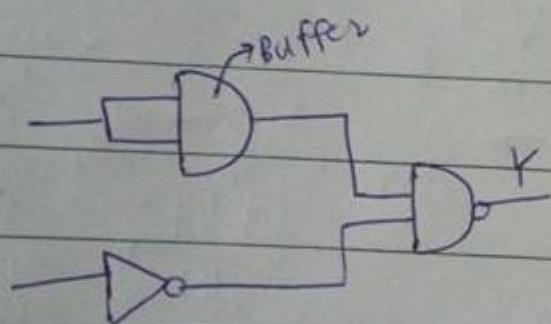
\* centre neglect  
product of side  
capacitor same  
so balanced.







## Test discussion



$$\omega_L = \frac{C}{L} = \frac{2C}{3}$$

